

$$a. \frac{d}{dx} [\arcsin(5x)]$$

$$(a) \quad 5 / \sqrt{1 - (5x)^2}$$

$$(b) \quad e^x / 1 + (e^x)^2$$

$$b. \frac{d}{dx} [\arctan e^x]$$

$$c. \frac{d}{dx} \left[ \operatorname{arcsec} \frac{x}{2} \right]$$

$$c. \quad \frac{d}{dx} \sec^{-1} \left( \frac{x}{2} \right) = \frac{1}{\frac{x}{2} \sqrt{\left( \frac{x}{2} \right)^2 - 1}} \cdot \frac{1}{2} \Rightarrow \frac{1}{2x \sqrt{\left( \frac{x}{2} \right)^2 - 1}}$$

$$d. \frac{d}{dx} [\arcsin x + x\sqrt{1-x^2}]$$

d)  $f(x) = \arcsin x + x\sqrt{1-x^2}$

~~$f'(x) = \frac{1}{\sqrt{1-x^2}} + \sqrt{1-x^2} + x \cdot \frac{-2x}{2\sqrt{1-x^2}}$~~

~~$f'(x) = \frac{1}{\sqrt{1-x^2}} + \frac{\sqrt{1-x^2}}{1} - \frac{2x^2}{2\sqrt{1-x^2}}$~~

$$f'(x) = \frac{1}{\sqrt{1-x^2}} + \frac{\sqrt{1-x^2}}{1} - \frac{2x^2}{2\sqrt{1-x^2}}$$

$$= \frac{1 + 2(1-x^2) - x^2}{2\sqrt{1-x^2}}$$

$$f'(x) = \frac{2+2x^2}{\sqrt{1-x^2}}$$

$$\textcircled{39} \quad x^3 + y^3 = 1$$

$$\frac{d}{dx}(x^3 + y^3) = \frac{d}{dx}(1)$$

$$\cancel{3}x^2 + \cancel{3}y^2 \frac{dy}{dx} = \cancel{0}$$

$$\frac{0}{3}$$

$$x^2 + y^2 \frac{dy}{dx} = 0$$

$$\frac{-x^2}{y^2} = \frac{dy}{dx}$$

$$y^3 = 1 - x^3$$

$$\frac{d^2 y}{dx^2} = \frac{y^2(-2x) - (-x^2)2y \frac{dy}{dx}}{(y^2)^2}$$

$$\frac{d^2 y}{dx^2} = \frac{x^2 2y \frac{dy}{dx} - 2xy^2}{y^4}$$

$$\frac{-2xy^2}{y^4} + \frac{x^2 2y}{y^4} \cdot \left(\frac{-x^2}{y^2}\right)^{\frac{dy}{dx}}$$

$$\frac{y^2}{y^2} \cdot \frac{-2xy^2}{y^4} - \frac{x^4 2y}{y^6}$$

$$\frac{2xy}{y^4} - \frac{x^4 2y}{y^4}$$

$$\frac{-2xy^3 - 2x^4}{y^5}$$

$$\frac{-2x(1-x^3) - 2x^4}{y^5}$$

$$\frac{-2x + \cancel{2x^4} - \cancel{2x^4}}{y^5}$$

$$\frac{d^2 y}{dx^2} = \frac{-2x}{y^5}$$





